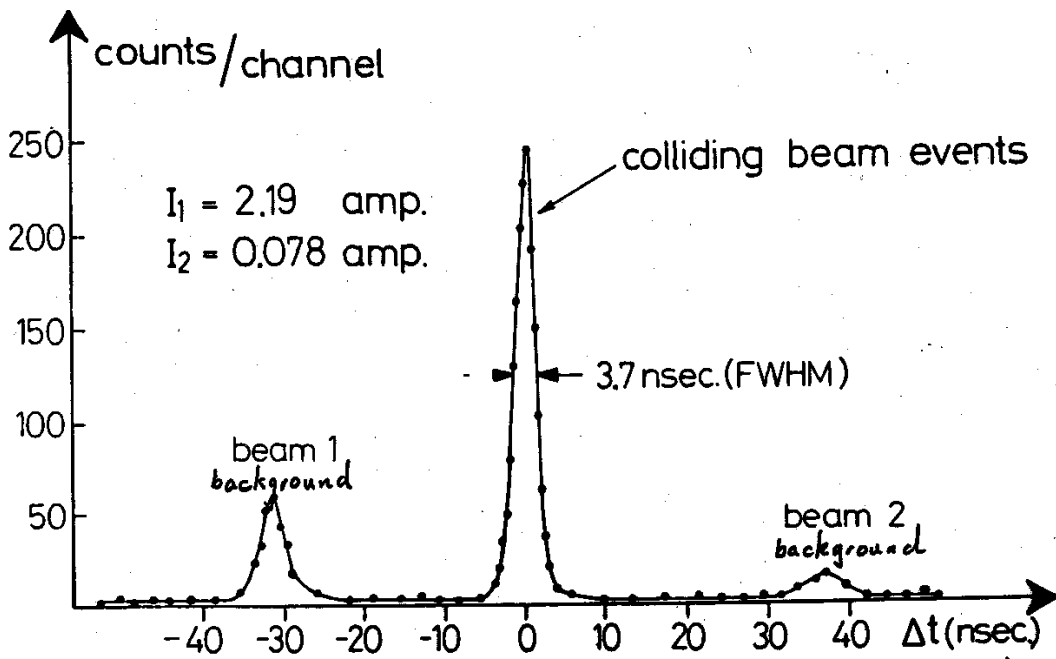
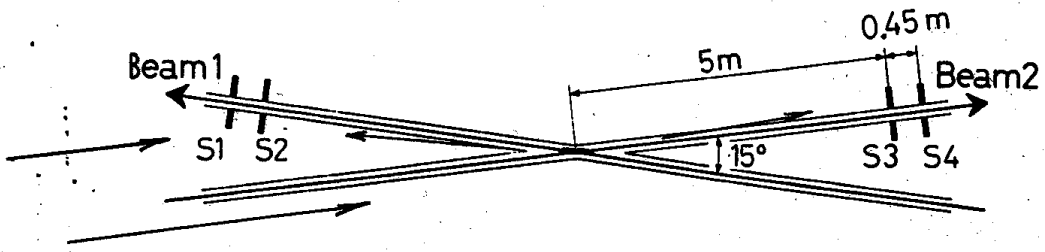
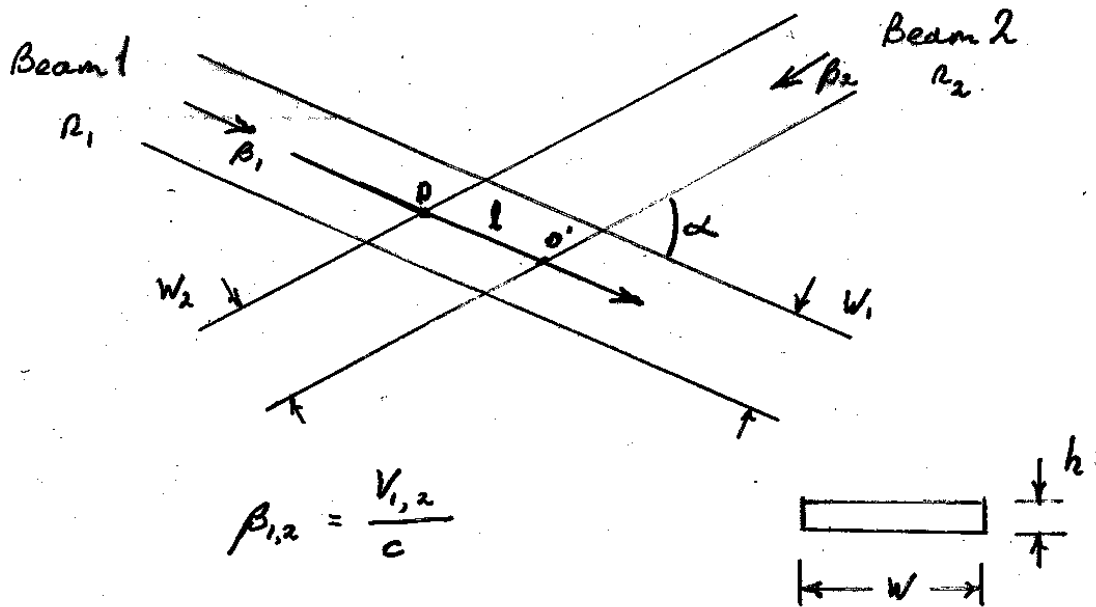


Luminosity Optimisation at the  
ISR.



## Coasting beams with crossing angle



Consider traversal of beam 2 by a single particle of beam 1

ISR luminosity depends only on circulating currents and  $h_{eff}$ .

eq. (26)

$$L = \frac{I_1 I_2}{c e^2 h_{\text{eff}} \tan \frac{\alpha}{2}}$$

is calculable

$I_1, I_2$  measured

and  $\frac{dR}{dt} = \sigma_M \cdot h$  allows  $\sigma_M$  to be found

hence, now have a calibrated monitor.

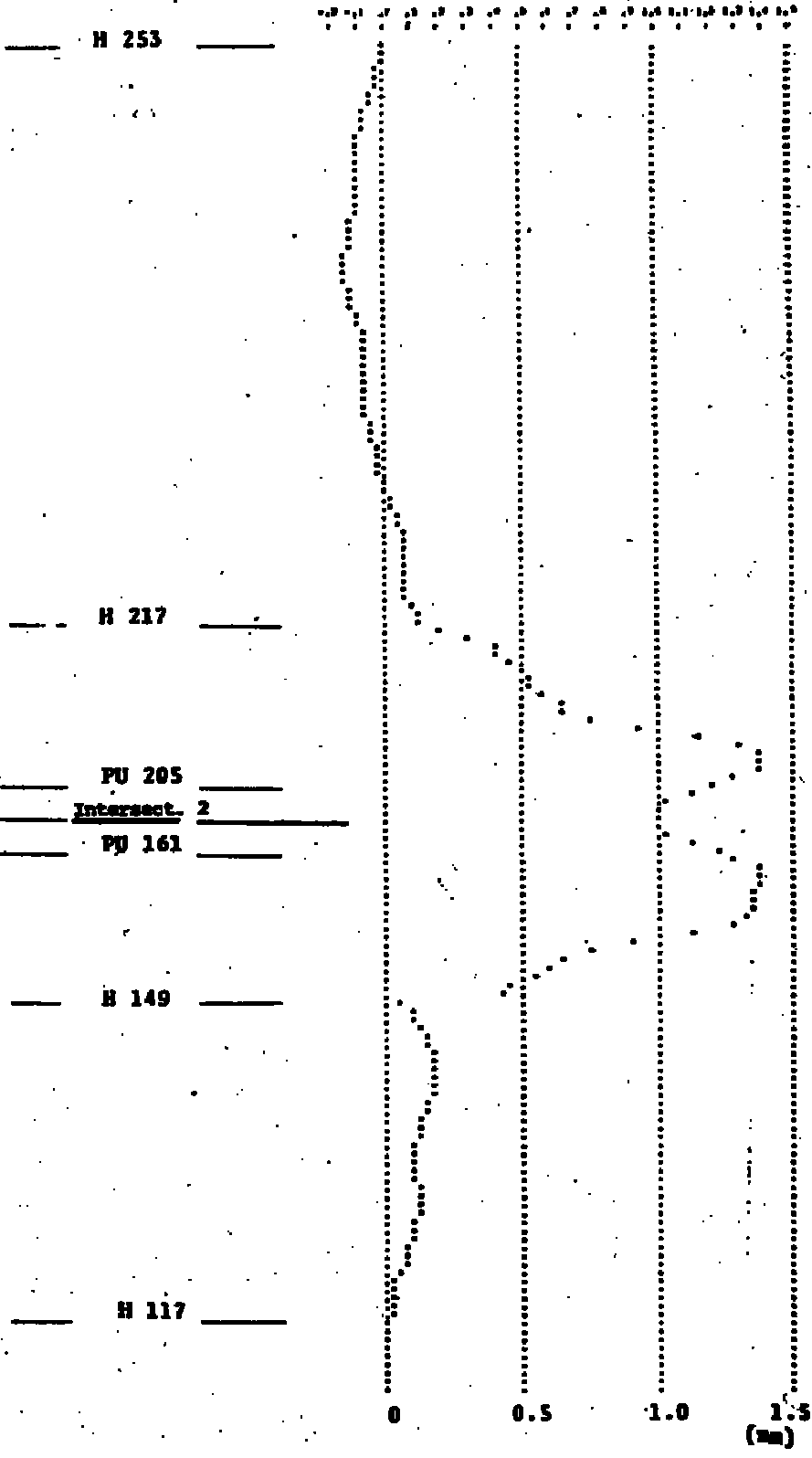
### Vertical Beam Displacements

Need accurate  $h$  scale

Horizontal field magnets  $\frac{1}{4} \lambda$  before and after the crossing point for optimisation.

For completely local bumps with variable  $Q_V$  need correcting magnets in addition.

REF: 100-100000  
100-100000



AGS tracking of 1 mm closed orbit bump

## The Van der Meer method

$$h_{\text{eff}} = \frac{\int_{-\infty}^{\infty} \rho_1 dz \int_{-\infty}^{\infty} \rho_2 dz}{\int_{-\infty}^{\infty} \rho_1 \rho_2 dz} \quad \text{equ (25)}$$

To maximise  $L$  need to minimise  $h_{\text{eff}}$  which requires zero separation between vertical beam centres.

Let the distance between vertical centres be  $h$

The counting rate in a (background free) monitor

will be 
$$A \int \rho_1(z) \rho_2(z-h) dz \quad (29)$$

where  $A$  is an unknown constant depending on the acceptance of the monitor and  $\sigma_i$ .

If this counting rate is plotted as a function of  $h$  a distribution of the following kind will be obtained.

Area under curve = 3000 counts.mm<sup>2</sup>

At  $h=0$  rate = 750 counts/sec

$$h_{\text{eff}} = \frac{3000}{750} = 4 \text{ mm}$$

Monitor  
Counts/sec

$$I_1 = 2.884 \text{ A}$$

$$I_2 = 2.524 \text{ A}$$

